

Warm-up:

Solve each quadratic equation by the quadratic formula.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Step 1: Set your equation equal to zero

Step 2: list a= b= c=

Step 3: Plug a, b, c into the formula

Step 4: Simplify

1) $x^2 + 22x + 121 = -22x$

$$x^2 + 22x + 121 = 0$$

$a = 1$ $b = 22$ $c = 121$

$$\frac{-22 \pm \sqrt{484 - 4(1)(121)}}{2(1)}$$

$$\frac{-22 \pm \sqrt{484 - 484}}{2}$$

$$\frac{-22 \pm 0}{2} \rightarrow \boxed{x = -11}$$

2) $-7w + 6 = -4w^2$

$$4w^2 - 7w + 6 = 0$$

$a = 4$ $b = -7$ $c = 6$

$$\frac{7 \pm \sqrt{49 - 4(4)(6)}}{2(4)}$$

$$\frac{7 \pm \sqrt{49 - 96}}{8}$$

$$\frac{7 \pm \sqrt{-47}}{8}$$

$$\boxed{\frac{7 \pm \sqrt{47} i}{8}}$$

- Discuss with your elbow partner: what does it mean to solve a system of equations?

It means to find points that are on all equations

Agenda:

- 1) Warm-up
- 2) Homework questions
- 3) New Lesson---3.5 Solving Nonlinear Systems
- 4) Homework/in-class activity

Algebra 2: 3.5 Solving Nonlinear Systems:

Learning Targets for Today:

- 1) Solve systems of nonlinear equations.
- 2) Solve quadratic equations by graphing.

(A) Solving a System of Nonlinear Equations

We have solved systems of linear equations by graphing, substitution and elimination earlier in the year! You can also use these methods to solve a system of nonlinear equations. In a nonlinear system, at least one of the equations is nonlinear. Example:

$$Y = 2x + 5 \quad (\text{line or linear})$$
$$Y = x^2 + 2x - 4 \quad (\text{not linear...it's a quadratic})$$

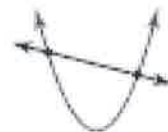
When the graphs of the equations in a system are a line and a parabola, the graphs can intersect in zero, one, or two points.



No solution



One solution



Two solutions

Example: Solving a nonlinear system by graphing

$$y = x^2 - 2x - 1$$

$$y = -2x - 1$$

$$Y = -2X - 1$$

line

$$m = \text{slope} = -\frac{2}{1}$$

$$b = Y\text{-int} = -1$$

$$Y = X^2 - 2X - 1$$

Quadratic in standard form

$$a = 1 \quad b = -2 \quad c = -1$$

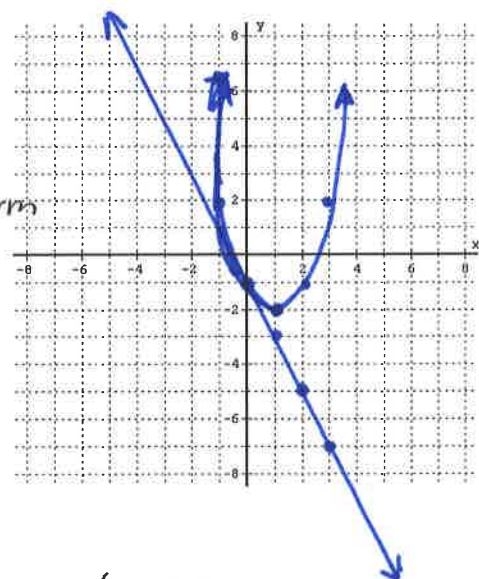
Vertex

$$-\frac{b}{2a} \rightarrow \frac{2}{2(1)} = \frac{2}{2} = 1$$

$$Y = (1)^2 - 2(1) - 1$$

$$1 - 2 - 1$$

$$-2$$



Vertex (1, -2)

"a"-value = 1,

$$\Rightarrow \underline{\underline{(0, -1)}}$$

Try: Solve the nonlinear system by graphing

$$y = x + 2$$

$$y = \frac{1}{2}(x+2)^2$$

$$Y = X + 2$$

line

$$\text{slope} = \frac{1}{1}$$

$$Y\text{-int} = 2$$

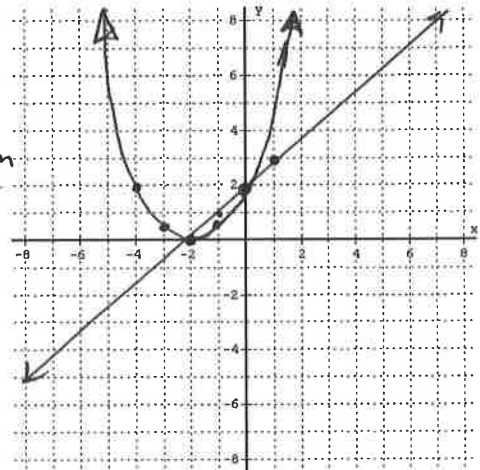
$$Y = \frac{1}{2}(x+2)^2$$

Quadratic in Vertex form

$$V(-2, 0)$$

$$\text{"a"-value} = \frac{1}{2}$$

2-Solutions $\rightarrow (0, 2) \text{ \& } (-2, 0)$



Try: Solve the nonlinear system by graphing

$$y = \frac{1}{3}x + 2$$

$$y = -3x^2 - 6x - 4$$

$$Y = \frac{1}{3}X + 2$$

line

$$\text{slope} = \frac{1}{3}$$

$$Y\text{-int} = 2$$

$$Y = -3x^2 - 6x - 4$$

Quadratic in standard

$$a = -3 \quad b = -6 \quad c = -4$$

Vertex

$$\frac{-b}{2a} \rightarrow \frac{6}{2(-3)} \Rightarrow \frac{6}{-6} = -1$$

$$Y = -3(-1)^2 - 6(-1) - 4$$

$$-3(1) + 6 - 4$$

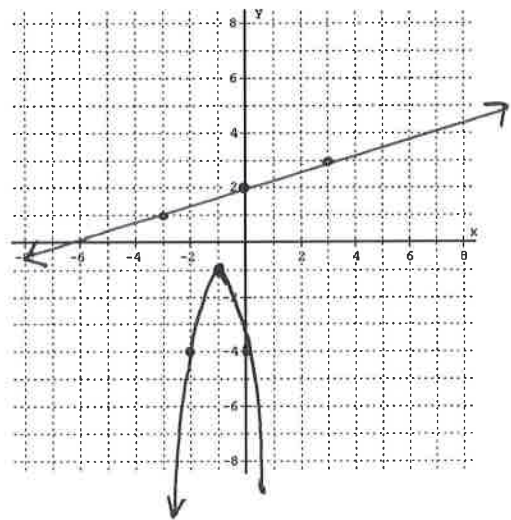
$$-3 + 6 - 4$$

$$3 - 4$$

$$-1$$

$$\text{Vertex } (-1, -1)$$

$$\text{"a"-value} = \frac{-3}{1}$$



NO SOLUTIONS

Example: Solving a nonlinear system by substitution

$$x^2 + x - y = -1$$

$$x + y = 4$$

Step 1: Solve one equation for either x or y

Step 2: Replace the letter you solved for in the other equation

Step 3: Solve your "new" one variable equation

Step 1 $x + y = 4$ ~~Let's~~ Lets solve for $y \rightarrow$ b/c look how easy it is to replace the y versus the two x 's...
 $y = -x + 4$

Step 2 $x^2 + x - (-x + 4) = -1$

Step 3 $x^2 + x + x - 4 = -1$

Now solve it!

$$x^2 + 2x - 3 = 0 \quad 3 \cdot 1$$

$$(x + 3)(x - 1) = 0$$

$$x + 3 = 0 \quad x - 1 = 0$$

$$x = -3 \quad x = 1$$

$$y = -x + 4$$

$$x = -3$$

$$y = -(-3) + 4$$

$$y = 3 + 4$$

$$y = 7$$

$$\underline{\underline{(-3, 7)}}$$

$$x = 1$$

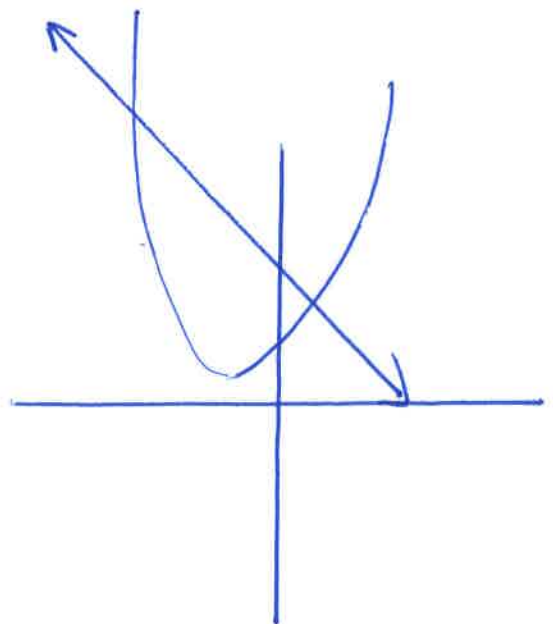
$$y = -(1) + 4$$

$$y = -1 + 4$$

$$y = 3$$

$$\underline{\underline{(1, 3)}}$$

These are the x -parts to the two solution points



Try: Solving a nonlinear system by substitution

$$x^2 + 2x - y = 5$$

$$2x + y = 7$$

Step 1 $y = -2x + 7$

Step 2 $x^2 + 2x - () = 5$

Step 3 $x^2 + 2x - (-2x + 7) = 5$
 $x^2 + 2x + 2x - 7 = 5$

$$x^2 + 4x - 12 = 0$$

$\frac{12 \cdot 1}{6 \cdot 2}$
 $\frac{4 \cdot 3}{4 \cdot 3}$

$$(x + 6)(x - 2) = 0$$

$$x + 6 = 0 \quad x - 2 = 0$$

$$x = -6 \quad x = 2$$

$$y = -2x + 7$$

$$x = -6$$

$$x = 2$$

$$y = -2(-6) + 7$$

$$y = -2(2) + 7$$

$$12 + 7$$

$$y = -4 + 7$$

$$19$$

$$3$$

$$(-6, 19)$$

$$(3, 2)$$

Try: Solving a nonlinear system by substitution

$$x^2 + 3x + y = 0$$

$$2x + y = 5$$

Step 1 $y = -2x + 5$

Step 2 $x^2 + 3x + () = 0$

$$x^2 + 3x + (-2x + 5) = 0$$

Step 3 $x^2 + x + 5 = 0$
doesn't factor...

$$a = 1 \quad b = 1 \quad c = 5$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-1 \pm \sqrt{1 - 4(1)(5)}}{2(1)}$$

$$\frac{-1 \pm \sqrt{1 - 20}}{2}$$

imaginary \rightarrow No real solutions

$$\frac{-1 \pm \sqrt{-19}}{2}$$

Example: Solving a nonlinear system by elimination

$$2x^2 - 5x - y = -2$$

$$x^2 + 2x + y = 0$$

Step 1: Line your equations up (x above x, y above y, x^2 above x^2 ...)

Step 2: Eliminate all x's or all y's (so your equation only has one variable)

- You might need to multiply an equation by a number to make them add to zero

Step 3: Solve the remaining one-variable equation

Step 1

$$\begin{array}{r} 2x^2 - 5x - y = -2 \\ x^2 + 2x + y = 0 \end{array}$$

already lined up
& the y's add to zero

Step 2

$$3x^2 - 3x = -2$$

Step 3

$$3x^2 - 3x + 2 = 0$$

$a=3$ $b=-3$ $c=2$

$$\frac{3 \pm \sqrt{9 - 4(3)(2)}}{2(3)}$$

$$\frac{3 \pm \sqrt{9 - 24}}{6}$$

$$\frac{3 \pm \sqrt{-15}}{6}$$

→ NO SOLUTIONS

Try: Solving a nonlinear system by elimination

$$3x^2 + 2x - 2y = 10$$

$$x^2 - 6x + 2y = -12$$

Step 1

$$\begin{array}{r} 3x^2 + 2x - 2y = 10 \\ x^2 - 6x + 2y = -12 \\ \hline \end{array}$$

Step 2

$$4x^2 - 4x = -2$$

Step 3

$$4x^2 - 4x + 2 = 0$$

$a = 4 \quad b = -4 \quad c = 2$

$$\frac{4 \pm \sqrt{16 - 4(4)(2)}}{2(4)}$$

$$\frac{4 \pm \sqrt{16 - 32}}{8}$$

$$\frac{4 \pm \sqrt{-16}}{8}$$

No Solutions

Try: Solving a nonlinear system by elimination

$$2x^2 + 4x - y = -2$$

$$x^2 + y = 2$$

Step 1

$$\begin{array}{r} 2x^2 + 4x - y = -2 \\ x^2 + y = 2 \\ \hline \end{array}$$

Step 2

$$3x^2 + 4x = 0$$

Step 3

Lets factor. Common Term

$$x(3x + 4) = 0$$

$$x = 0 \quad 3x + 4 = 0$$

$$x = 0 \quad x = -4/3$$

Finding y-parts

$$x^2 + y = 2$$

$$x = 0$$

$$(0)^2 + y = 2$$

$$y = 2$$

$$(0, 2)$$

$$x = -4/3$$

$$\left(-\frac{4}{3}\right)^2 + y = 2$$

$$\frac{16}{9} + y = 2$$

$$y = 2 - \frac{16}{9}$$

$$y = \frac{18}{9} - \frac{16}{9}$$

$$y = \frac{2}{9}$$

$$\left(-\frac{4}{3}, \frac{2}{9}\right)$$

Homework: Pg. 136 (3-5, 11, 12, 15-17, 27-29)