

Warm-up:

$$f(x) = x^2$$

$$g(x) = x-3$$

Find:

1)  $f + g$

$$(x^2) + (x-3)$$

$$\boxed{x^2 + x - 3}$$

2)  $f - g$

$$(x^2) - (x-3)$$

$$\boxed{x^2 - x + 3}$$

3)  $f(x) \cdot g(x)$

$$x^2 \overbrace{(x-3)}$$

$$\boxed{x^3 - 3x^2}$$

4)  $\frac{f(x)}{g(x)}$

$$\frac{x^2}{x-3}$$

$$D: x \neq 3$$

5)  $f(g(x))$

$$(x-3)^2$$

or  
 $(x-3)(x-3)$

$$\underline{x^2 - 6x + 9}$$

6)  $g(f(x))$

$$(x^2) - 3$$

$$\boxed{x^2 - 3}$$

Agenda:

- 1) Warm-up (check w/ elbow partner)
- 2) Homework Questions
- 3) New Lesson on 5.6 Inverses
- 4) In class Activity/Homework

## 5.6 Inverse of a Function:

### Learning Targets:

- 1) Find the inverse of a Function
- 2) Verify inverses of Functions

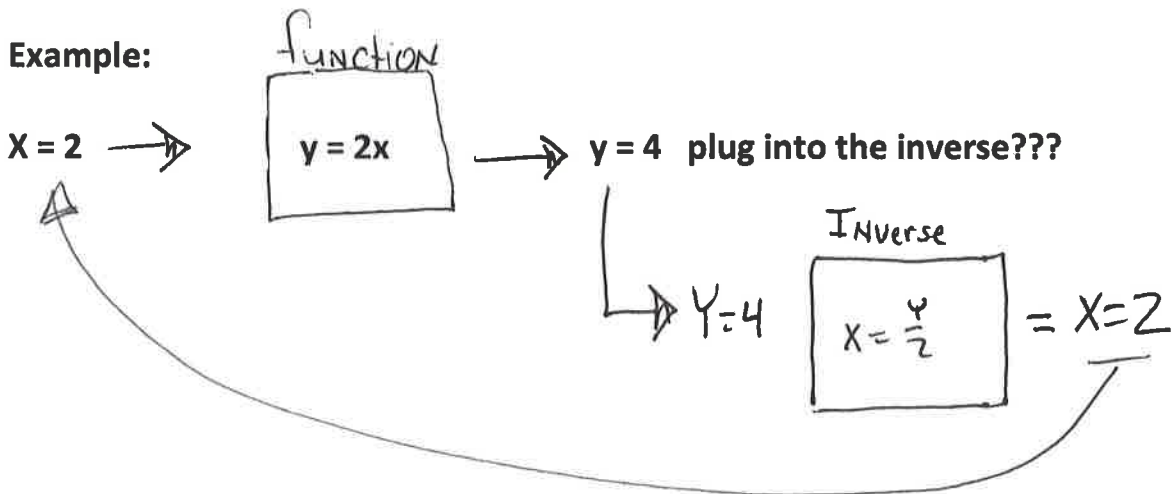
### (A) Inverse Functions:

An inverse undoes what the original function did.

Example:

\*Clothes...getting dressed

Example:



**(B) Finding an inverse:**

To find the inverse of an equation...

**Step 1: Switch the x's and y's**

**Step 2: solve for y**

Example:  $Y = 2x - 4$   
switch

$$X = 2y - 4$$
$$\begin{array}{ccc} +4 & & +4 \end{array}$$
$$\frac{X+4}{2} = \frac{2y}{2}$$

$$y = \frac{X+4}{2} \quad \text{OR} \quad y = \frac{1}{2}X + 2$$

Try:  
Find the inverse of:

1)  $y = -3x + 6$

$$X = -3y + 6$$
$$\begin{array}{ccc} -6 & & -6 \end{array}$$

$$\frac{X-6}{-3} = \frac{-3y}{-3}$$

$$y = \frac{X-6}{-3} \quad \text{OR} \quad y = \frac{1}{3}X + 2$$

2)  $y = \frac{1}{2}x - 2$

$$X = \frac{1}{2}y - 2$$
$$\begin{array}{ccc} +2 & & +2 \end{array}$$

$$2 \cdot (X+2) = \left(\frac{1}{2}y\right) \cdot 2$$

$$y = 2X + 4$$

3)  $y = \frac{-3}{7}x + \frac{2}{7}$

$$X = \frac{-3}{7}y + \frac{2}{7}$$

\* clear fractions

$$7X = -3y + 2$$
$$\begin{array}{ccc} -2 & & -2 \end{array}$$

$$7X - 2 = -3y$$

$$\frac{-3y}{-3} = \frac{7X-2}{-3}$$

$$y = \frac{-7}{3}X + \frac{2}{3}$$

Switch for  $X \leftrightarrow Y$

(c) What inverses look like:

Example  $Y = X^2$

1) Table form:

X	Y
-1	1
0	0
1	1
2	4



X	Y
1	-1
0	0
1	1
4	2

2) equation form

$$y = x^2$$

↙ ↘

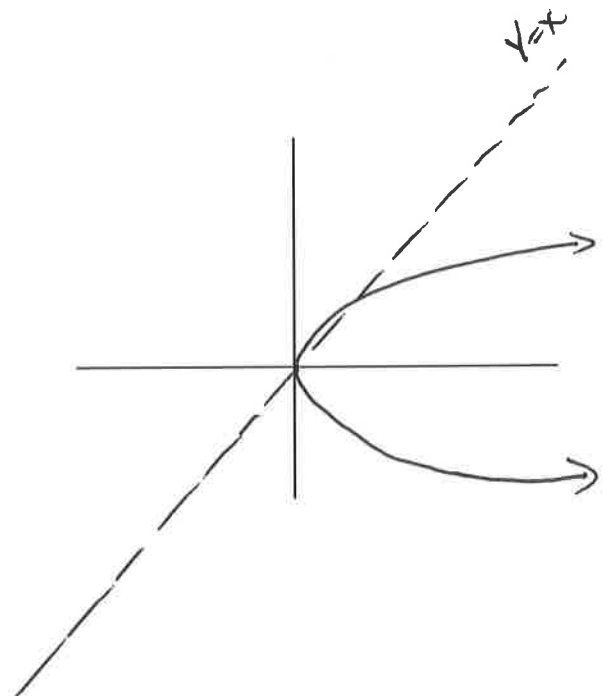
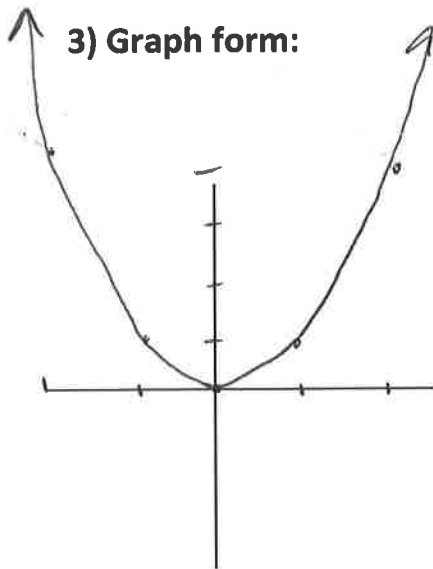
$$x = y^2$$

↘ ↙

$$\sqrt{y^2} = \sqrt{x}$$

→

$$\underline{\underline{y = \pm \sqrt{x}}}$$



**(D) Verifying Inverse Functions:**

To verify that 2 functions  $f$  and  $g$  are inverses:

1)  $f(g(x)) = x$  AND      2)  $g(f(x)) = x$

Both must be true to prove that  $f$  &  $g$  are inverses of each other.

Example:

Verify that  $f(x) = 2x - 4$  and  $g(x) = \frac{1}{2}x + 2$  are inverses

$$f \circ g = 2\left(\frac{1}{2}x + 2\right) - 4 \rightsquigarrow x + 4 - 4 = x \quad \checkmark$$

$$g \circ f = \frac{1}{2}(2x - 4) + 2 \rightsquigarrow x - 2 + 2 = x \quad \checkmark$$

This proves they are inverses!

Try:

Verify that  $f(x) = -3x + 6$  and  $f^{-1}(x) = \frac{-1}{3}x + 2$  are inverses

$$f \circ g = -3\left(\frac{-1}{3}x + 2\right) + 6 \rightsquigarrow x - 6 + 6 \rightarrow x$$

$$g \circ f = \frac{-1}{3}(-3x + 6) + 2 \rightsquigarrow x - 2 + 2 \rightarrow x$$

(E) Finding inverses of non-linear functions

Step 1: replace  $f(x)$  with  $y$

Step 2: switch  $x$  and  $y$

Step 3: solve for  $y$

Example:

$$\begin{aligned} f(x) &= x^2 \\ y &= x^2 \\ x &= y^2 \quad \text{or} \end{aligned} \quad \begin{array}{l} \rightarrow \sqrt{y^2} = \sqrt{x} \\ \boxed{y = \pm\sqrt{x}} \end{array}$$

Try:

$$\begin{aligned} f(x) &= x^5 \\ y &= x^5 \\ x &= y^5 \end{aligned} \quad \begin{array}{l} \rightarrow \sqrt[5]{y^5} = \sqrt[5]{x} \\ \boxed{y = \sqrt[5]{x}} \end{array}$$

Try:

$$\begin{aligned} f(x) &= \frac{1}{2}x^3 - 2 \\ y &= \frac{1}{2}x^3 - 2 \\ x &= \frac{1}{2}y^3 - 2 \end{aligned} \quad \begin{array}{l} \rightarrow \frac{1}{2}y^3 - 2 = x \quad +2 \\ \quad \quad \quad +2 \\ 2 \left( \frac{1}{2}y^3 \right) = (x+2) \\ \sqrt[3]{y^3} = \sqrt[3]{2x+4} \\ \boxed{y = \sqrt[3]{2x+4}} \end{array}$$